

H_∞

State estimation Stochastic neutral type neural networks with time varying delays and Markovian Jumping Parameters

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1. INTRODUCTION & OBJECTIVE

The delay-dependent design of H_∞ State estimation Stochastic neutral type neural networks with time varying delays and Markovian Jumping Parameters is considered in this paper. By constructing a suitable Lyapunov-Krasovskii functional, a delay-dependent condition is established to guarantee the estimation error systems to be asymptotical mean-square stable and achieve a prescribed H_∞ performance index. Both delay-dependent and delay-independent sufficient conditions for the existence of desired state estimators are derived in terms of linear matrix inequalities (LMIs) to guarantee the Markov jump delayed neural networks to be passive. Passivity and Passification problems are tackled by using mode-dependent. Finally, a numerical example demonstrates that the proposed approaches are effective.

2. RESULTS & HIGHLIGHTS OF IMPORTANT POINTS

The problem of H_∞ performance state estimation for stochastic neutral type neural networks with time varying delays and Markovian jumping parameters has been investigated in this paper. Delay-dependent and delay-independent design criteria have been established. Our future research topics would include the following issues:

- (1). To remove the restriction of the derivative of delay $\mu < 1$;
- (2). The H_∞ state estimation for stochastic neural networks with Markovian jump parameters or mixed time-varying delays, discrete-time stochastic neural networks, stochastic genetic regulatory networks and neutral stochastic neural networks;

(3). The generalized H_∞ state estimation problem for stochastic neural networks.

Numerical Example

In this section, an example is given to demonstrate the effectiveness of the proposed method. Consider a three-neuron stochastic neural network (1)-(3) with parameters:

$$\begin{aligned}
 A_1 &= \begin{bmatrix} 2 & 0 \\ 0 & 3 \end{bmatrix}, W_{01} = \begin{bmatrix} -0.4 & -0.2 \\ 0.3 & -0.2 \end{bmatrix}, W_{11} = \begin{bmatrix} -0.2 & -0.1 \\ 0.1 & 0.2 \end{bmatrix}, W_{21} = \begin{bmatrix} -0.2 & -0.9 \\ -0.9 & 0.25 \end{bmatrix}, \\
 B_{11} &= \begin{bmatrix} 0.3 & -0.2 \\ -0.2 & 0.5 \end{bmatrix}, B_{21} = \begin{bmatrix} -0.4 & 0.3 \\ 0.2 & 0.4 \end{bmatrix}, H_{11} = \begin{bmatrix} 0.2 & 0.2 \\ 0.2 & 0.8 \end{bmatrix}, C_1 = \begin{bmatrix} -0.2 & 0.1 \\ 0.8 & 0.7 \end{bmatrix}, \\
 H_{21} &= \begin{bmatrix} 0.2 & -0.6 \\ -0.6 & 0.6 \end{bmatrix}, D_1 = \begin{bmatrix} -0.2 & 0.3 \\ 0.4 & 0.1 \end{bmatrix}, L = \begin{bmatrix} 0.3 & 0.4 \\ 0.5 & 0.8 \end{bmatrix}, \Sigma_1 = 0, \Sigma_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \\
 F_1 &= 0, F_2 = \begin{bmatrix} -0.5 & 0 \\ 0 & -0.5 \end{bmatrix}, I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}.
 \end{aligned}$$

Using Matlab LMI Toolbox to solve the LMI in Theorem 2, we obtain the solutions as follows:

$$\begin{aligned}
 P_1 &= \begin{bmatrix} 0.2937 & 0.0702 \\ 0.0702 & 0.2362 \end{bmatrix}, Q = \begin{bmatrix} -2.9391 & -0.3554 \\ -0.3554 & -3.4313 \end{bmatrix}, R = \begin{bmatrix} 1.9398 & -0.3190 \\ -0.3190 & 1.7739 \end{bmatrix}, \\
 R_1 &= \begin{bmatrix} -2.0117 & -0.0125 \\ -0.0125 & -2.0060 \end{bmatrix}, Z = \begin{bmatrix} -0.4324 & 0.1453 \\ 0.1453 & -0.4212 \end{bmatrix}, T_1 = \begin{bmatrix} 0.0203 & -0.1783 \\ -0.1783 & -0.2678 \end{bmatrix}, \\
 \lambda_1 &= 1.1289, \lambda_2 = 1.1389.
 \end{aligned}$$

By Theorem 3.2, when $\mu = 1.6$, $\tau = 0.925$, $\gamma = 1.14570$, $h_d = 1.2$, gain the matrix of (44) can be designed as:

$$K_1 = \begin{bmatrix} 0.2686 & -0.3618 \\ -0.8347 & -1.0263 \end{bmatrix}$$

REFERENCES

1. H. Gao, W. Sun, P. Shi, *Robust sampled-data H_∞ control for vehicle active suspension systems*, *IEEE Trans. Control Syst. Technol.* 10(1) (2010) 238–245.
2. A. Cichocki, R. Unbehauen, *Neural Networks for Optimization and Signal Processing*, Chichester: Wiley, (1993).
3. S. Arik, *An analysis of exponential stability of delayed neural networks with time-varying delays*, *Neural Networks* 17(2004) 1027–1031.
4. M. Belli, M. Conti, P. Crippa, and C. Turchetti, *Artificial neural networks as approximators of stochastic process*, *Neural Networks* 12(1999) 647–658.
5. Y. Ding, H. Liu, and K. Shi, *H_∞ state-feedback controller design for continuous-time*

nonhomogeneous Markov jump systems. *Optimal Control Applications and Methods* 38(2016)133–144